On polynomial numerical hulls of matrices

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Let M_n be the set of $n \times n$ complex matrices. For any $A \in M_n$, we use the joint numerical range $W(A, A^2, \ldots, A^l)$ to study the polynomial numerical hull of order l of A, denoted by $V^l(A)$. By considering the k-rank joint numerical hulls $\Lambda_k(A, A^2, \ldots, A^l)$, we introduce the k-rank polynomial numerical hull of order l of a matrix A, which is defined and denoted by

$$V_k^l(A) = \{ \lambda \in \Lambda_k(A) : (\lambda, \lambda^2, \dots, \lambda^l) \in \text{conv} [\Lambda_k(A, A^2, \dots, A^l)] \}.$$

We study some relationship between these two notations.

Key words: higher rank numerical range, joint numerical range, polynomial numerical hull.

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